

Inequality and Macroeconomics: Facts and Theories

Lecture 3. Neoclassical macro models of inequality: bringing together theory and facts

Fabrizio Perri

Minneapolis FED and CEPR



KU Leuven

May 2024

The question

- 1 Is **household income and wealth inequality** quantitatively important for **aggregate consumption, investment and output** response to an exogenous **Great Recession** shock?
- 2 How do **social insurance policies** impact these **aggregates**?
- 3 How are consumption, welfare losses of aggregate shock **distributed** across population? How does **social insurance** affect that **distribution**?

Why inequality matters for dynamics of recessions?

- ▷ Earnings fall in recessions (unemployment rises, wages fall)
- ▷ If low wealth households have higher MPC out of current earnings changes....
- ▷ ...then the degree of **wealth inequality** impacts **aggregate C dynamics** over the cycle.
- ▷ If, in addition, **aggregate C matters for output** (if Y is partially demand-determined b/c of endogenous TFP, nominal rigidities), then **wealth distribution influences aggregate Y** dynamics...
- ▷ ...and **social insurance policies** are potentially **output-stabilizing**.

Data meets Quantitative Theory

- ▶ *Empirical analysis using US household (PSID) y , c , a data:*
 - ▶ How did y , c , a distribution look prior to Great Recession?
 - ▶ How did y , c , a change for individual households in the Great Recession?

Data meets Quantitative Theory

- ▶ *Empirical analysis using US household (PSID) y, c, a data:*
 - ▶ How did y, c, a distribution look prior to Great Recession?
 - ▶ How did y, c, a change for individual households in the Great Recession?
- ▶ *Quantitative analysis* using versions of heterogeneous household business cycle (Krusell & Smith 1998) model:
 - ▶ Does the model match the inequality facts?
 - ▶ Does wealth distribution matter (quantitatively) for response of C, I to Great Recession shock?
 - ▶ What about Y response if Y is partially (aggregate consumption C) demand-determined?

Data meets Quantitative Theory

- ▶ **Empirical analysis using US household (PSID) y, c, a data:**
 - ▶ How did y, c, a distribution look prior to Great Recession?
 - ▶ How did y, c, a change for individual households in the Great Recession?
- ▶ **Quantitative analysis** using versions of heterogeneous household business cycle (Krusell & Smith 1998) model:
 - ▶ Does the model match the inequality facts?
 - ▶ Does wealth distribution matter (quantitatively) for response of C, I to Great Recession shock?
 - ▶ What about Y response if Y is partially (aggregate consumption C) demand-determined?
- ▶ **Policy analysis using** stylized unemployment insurance (UI) system:
 - ▶ How does UI impact $\Delta C, \Delta Y$ for given wealth distribution?
 - ▶ How does size of UI impact the wealth distribution itself?
 - ▶ How is distribution of welfare losses from Great Recession shaped by UI?

The data

- ▶ PSID waves of 2004-2006-2008-2010. Detailed US household-level information about y , c , a .
 - ▶ Panel dimension: can assess how individual households changed actions (c expenditures) during the Great Recession
 - ▶ Coarse time series dimension (biannual surveys for data between 2004 and 2010)

The data

- ▶ Variables of Interest

- ▶ Net Worth = a = Value of all assets (including real estate) minus liabilities
- ▶ Disposable Income = y = Total money income net of taxes (computed using TAXSIM)
- ▶ Consumption Expenditures = c = Expenditures on durables, nondurables and services (excluding health)

- ▶ Sample

- ▶ All households in PSID waves 2004-2006-2008-2010, with at least one member of age 22-60

Data: Marginal Distributions

| | y | c | a | SCF 07 a |
|---------------|--------|--------|---------|----------|
| Mean (2006\$) | 62,549 | 43,980 | 291,616 | 497,747 |
| %Share : Q1 | 4.5 | 5.6 | -0.9 | -0.2 |
| Q2 | 9.9 | 10.7 | 0.8 | 1.2 |
| Q3 | 15.3 | 15.6 | 4.4 | 4.6 |
| Q4 | 22.8 | 22.4 | 13.0 | 11.9 |
| Q5 | 47.5 | 45.6 | 82.7 | 82.5 |
| 90 – 95 | 10.8 | 10.3 | 13.7 | 11.1 |
| 95 – 99 | 12.8 | 11.3 | 22.8 | 25.3 |
| Top 1% | 8.0 | 8.2 | 30.9 | 33.5 |
| Sample Size | 6442 | | | 2910 |

- ▷ **a**: Bottom 40% holds basically no wealth
- ▷ **y, c**: less concentrated
- ▷ **a** distribution in PSID \simeq SCF except at very top

Heterogeneity (Inequality) in 2006: Joint Distributions

| Q.a | % Share of: | | Exp.Rate c/y (%) |
|-----|-------------|------|---------------------|
| | y | c | |
| Q1 | 8.6 | 11.3 | 92.2 |
| Q2 | 10.7 | 12.4 | 81.3 |
| Q3 | 16.6 | 16.8 | 70.9 |
| Q4 | 22.6 | 22.4 | 69.6 |
| Q5 | 41.4 | 37.2 | 63.1 |

- ▷ a correlated with y and saving
- ▷ Wealth-rich earn more and save at a higher rate
- ▷ Bottom 40% hold no wealth, still account for almost 25% of spending

Moving to the theory

- ▶ Empirical evidence shows:
 - ▶ Bottom 40% have no wealth...
 - ▶ ...but account for almost 25% of consumption

Moving to the theory

- ▶ Empirical evidence shows:
 - ▶ Bottom 40% have no wealth...
 - ▶ ...but account for almost 25% of consumption
- ▶ Is a standard macro model with heterogeneous agents a la Krusell & Smith (1998) consistent with these facts?
- ▶ We then use the model as a laboratory for *quantifying*:
 - ▶ how **wealth distribution** affects C, I, Y responses to Great Recession shock
 - ▶ how this impact is shaped by **social insurance policies**
 - ▶ how welfare losses from Great Recession are distributed across **wealth distribution**

Model: Summary of Key Elements

- ▶ Augmented Krusell and Smith (1998) model, similar to Carroll, Slacalek, Tokuoka & White (2015)
- ▶ Exogenous **aggregate shock Z** moves aggregate wages w and unemployment rate $\Pi_Z(u)$. Rare but severe (Y drops $\approx 7\%$ below trend) and persistent (22 quarters) recessions.

$$\begin{aligned} Y &= Z^* K^\alpha N(Z)^{1-\alpha} \\ Z^* &= Z C^\omega \end{aligned}$$

- ▶ **Aggregate consumption C** demand externality $\omega \geq 0$. (NK block)
- ▶ Exogenous **individual income risk**
 - ▶ Unemployment risk $s \in \{u, e\}$. Increases in recessions (8.4% vs. 5.3%).
 - ▶ Income risk y , conditional on being employed.
- ▶ **Individual preference heterogeneity**
- ▶ **Constant retirement (with social security) and survival risk age heterogeneity.**
- ▶ **Unemployment insurance system**

Aggregate Technology

- ▶ Standard production function

$$Y = Z^* K^\alpha N^{1-\alpha}$$

- ▶ Total factor productivity Z^* in turn is given by

$$Z^* = ZC^\omega$$

- ▶ C is aggregate consumption
 - ▶ $\omega \geq 0$: aggregate demand externality
 - ▶ Benchmark model $\omega = 0$
- ▶ Focus on $Z \in \{Z_l, Z_h\}$: recession and expansion.

$$\pi(Z'|Z) = \begin{pmatrix} \rho_l & 1 - \rho_l \\ 1 - \rho_h & \rho_h \end{pmatrix}.$$

- ▶ Capital depreciates at a constant rate $\delta = 0.025$ quarterly.
- ▶ Capital share: $\alpha = 36\%$

Household Preferences

- ▶ Continuum of households with **idiosyncratic y risk**
- ▶ **Period utility function** $u(c) = \log(c)$
- ▶ **To generate sufficient wealth dispersion** follow Carroll, Slacalek & Tokuoka (2015):
 - ▶ Households draw **discount factor** β at birth from $U[\bar{\beta} - \epsilon, \bar{\beta} + \epsilon]$
 - ▶ Choose $\bar{\beta}, \epsilon$ to match quarterly $K/Y = 10.26$, Wealth Gini of working pop.=0.77.
- ▶ In working life, constant retirement prob. $1 - \theta = 1/160$ (40 yrs of working life).
- ▶ In retirement constant death probability $1 - \nu = 1/60$ (15 yrs of retirement)

Household Preferences

- ▶ Continuum of households with **idiosyncratic y risk**
- ▶ **Period utility function** $u(c) = \log(c)$
- ▶ **To generate sufficient wealth dispersion** follow Carroll, Slacalek & Tokuoka (2015):
 - ▶ Households draw **discount factor** β at birth from $U[\bar{\beta} - \epsilon, \bar{\beta} + \epsilon]$
 - ▶ Choose $\bar{\beta}, \epsilon$ to match quarterly $K/Y = 10.26$, Wealth Gini of working pop.=0.77.
- ▶ In working life, constant retirement prob. $1 - \theta = 1/160$ (40 yrs of working life).
- ▶ In retirement constant death probability $1 - \nu = 1/60$ (15 yrs of retirement)
- ▶ Other mechanisms to generate large **wealth dispersion**
 - ▶ **Entrepreneurs** [Quadrini 1997]
 - ▶ **Bequest motives** [De Nardi 2004]
 - ▶ **Health expenditure shocks in old age** [De Nardi, French, Jones 2010, Ameriks, Briggs, Caplin, Shapiro, Tonetti 2015]
 - ▶ **Extreme income realizations** [Castaneda, Diaz-Gimenez, Rios-Rull 2003]
 - ▶ **Heterogeneous investm. returns** [Benhabib, Bisin, Zhu 2011]
 - ▶ **Wealth in utility** [Gaillard, Hellwig, Wangner, Werquin 2024]

Household Endowments

- ▶ Time endowment normalized to 1
- ▶ Idiosyncratic unemployment risk, $s \in S = \{u, e\}$
 - ▶ $\pi(s'|s, Z', Z)$
- ▶ Idiosyncratic labor productivity risk, $y \in Y$
 - ▶ Estimate stochastic process from annual PSID (1967-1996) data (only employed households):

$$\begin{aligned}\log(y') &= p + \epsilon \\ p' &= \phi p + \eta\end{aligned}$$

with persistence ϕ , innovations (η, ϵ) . Find estimates of $(\hat{\phi}, \hat{\sigma}_\eta^2, \hat{\sigma}_\epsilon^2) = (0.9695, 0.0384, 0.0522)$

- ▶ Turn into quarterly process, discretize into Markov chain

Government Policy

- ▷ Balanced budget unemployment insurance system
 - ▷ Replacement rate $\rho = \frac{b(y, Z, \Phi)}{w(Z, \Phi)y}$ if $s = u$
 - ▷ Thus benefits given by $b(y, Z, \Phi) = \rho w(Z, \Phi)y$
 - ▷ Baseline $\rho = 0.5$. Compare to $\rho = 0.1$.
 - ▷ Proportional labor income tax $\tau(Z; \rho)$ to balance budget:
- ▷ Balanced PAYGO social security system
 - ▷ Payroll tax rate $\tau_{SS} = 15.3\%$
 - ▷ Lump-sum benefits that balance the budget

Recursive Formulation of HH Problem

- ▷ Individual state variables $x = (y, s, a, \beta)$
- ▷ Aggregate state variables (Z, Φ)
- ▷ Aggregate law of motion $\Phi' = H(Z, \Phi, Z')$
- ▷ Household dynamic program problem of worker reads as

$$v_W(s, y, a, \beta; Z, \Phi) = \left\{ \max_{c, a' \geq 0} u(c) + \beta \sum_{(Z', s', y') \in (Z, S, Y)} \pi(Z'|Z) \pi(s'|s, Z', Z) \pi(y'|y) \right. \\ \left. * [\theta v_W(s', y', a', \beta; Z', \Phi') + (1 - \theta) v_R(a', \beta; Z', \Phi')] \right\}$$

subject to

$$c + a' = (1 - \tau(Z; \rho) - \tau_{SS}) w(Z, \Phi) y [1 - (1 - \rho) 1_u] + (1 + r(Z, \Phi) - \delta) a \\ \Phi' = H(Z, \Phi, Z')$$

Note that distribution is a state variable

Calibration of Aggregate Productivity Risk

- ▷ Recall that $Z \in \{Z_l, Z_h\}$ and

$$\pi(Z'|Z) = \begin{pmatrix} \rho_l & 1 - \rho_l \\ 1 - \rho_h & \rho_h \end{pmatrix}$$

- ▷ Expected *duration* of a recession is $EL_l = \frac{1}{1 - \rho_l}$. Fraction of time economy is in recession is

$$\Pi_l = \frac{1 - \rho_h}{2 - \rho_l - \rho_h}$$

- ▷ Choose $\rho_l, \rho_h, \frac{Z_l}{Z_h}$ to match:

- 1 the average length of a severe recession EL_l
- 2 the fraction of time economy is in severe recession, Π_l .
- 3 the decline in GDP per capita in *severe* recessions relative to normal times

What is a Severe Recession?

- ▷ Define start of severe recession when $u \geq 9\%$. Lasts as long as $u \geq 7\%$.
- ▷ From 1948 to 2014.III two severe recessions, 1980.II-1986.II and 2009.I-2013.III.
- ▷ Frequency of severe recessions: $\Pi_l = 16.48\%$, expected length of 22 quarters.
- ▷ Average unemployment rate $u(Z_l) = 8.39\%$, $u(Z_h) = 5.33\%$

- ▷ Implied transition matrix:

$$\pi = \begin{pmatrix} 0.9545 & 0.0455 \\ 0.0090 & 0.9910 \end{pmatrix}$$

- ▷ Average output drop in severe recessions measured as $\frac{Y_l}{Y_h} = 0.9298$. Matching this in model requires $\frac{Z_l}{Z_h} = 0.9614$.
- ▷ Severe recession similar in spirit to rare disasters [Rietz 1988, Barro 2006, Gourio 2015]

Idiosyncratic Employment status Transitions

Transition matrices $\pi(s'|s, Z', Z)$ for $s, s' \in \{u, e\}$ calibrated to quarterly job finding rates (computed from CPS). For example

- ▶ Economy is and remains in a recession: $Z = Z_l, Z' = Z_l$

$$\begin{pmatrix} 0.34 & 0.66 \\ 0.06 & 0.94 \end{pmatrix}$$

- ▶ Economy is and remains in normal times: $Z = Z_h, Z' = Z_h$

$$\begin{pmatrix} 0.19 & 0.81 \\ 0.05 & 0.95 \end{pmatrix}$$

- ▶ In recessions more likely to lose job and less likely to find one.
- ▶ Thus as economy falls into recession, UE risk up (and more persistent) even for those not yet having lost job. **Strong precautionary savings motive for wealth-poor!**

Versions of Model

- ① Original Krusell & Smith (1998) [KS] economy (single discount factor + income risk + low ρ)
- ② Economy 1 + heterogenous β 's, survival risk $\theta < 1$ and high $\rho = 50\%$ [Benchmark]
- ③ Economy 2 + aggregate demand externality $\omega > 0$

Inequality in the Benchmark Economy

| New Worth % Share held by: | Data | | Models | |
|-------------------------------|----------|---------|--------|------|
| | PSID, 06 | SCF, 07 | Bench | KS |
| Q1 | -0.9 | -0.2 | 0.3 | 6.9 |
| Q2 | 0.8 | 1.2 | 1.2 | 11.7 |
| Q3 | 4.4 | 4.6 | 4.7 | 16.0 |
| Q4 | 13.0 | 11.9 | 16.0 | 22.3 |
| Q5 | 82.7 | 82.5 | 77.8 | 43.0 |
| 90 – 95 | 13.7 | 11.1 | 17.9 | 10.5 |
| 95 – 99 | 22.8 | 25.3 | 26.0 | 11.8 |
| T1% | 30.9 | 33.5 | 14.2 | 5.0 |
| Gini | 0.77 | 0.78 | 0.77 | 0.35 |

- ▷ Benchmark economy does a good job matching bottom and top of wealth distribution, but still **misses very top**.
- ▷ Original KS economy does not produce enough inequality.

Joint Distributions (2006): data v/s model

| a Quintile | % Share of: | | | | | |
|------------|-------------|-------|------|-------|------|-------|
| | y | | c | | %c/y | |
| | Data | Model | Data | Model | Data | Model |
| Q1 | 8.6 | 6.0 | 11.3 | 6.6 | 92.2 | 90.4 |
| Q2 | 10.7 | 10.5 | 12.4 | 11.3 | 81.3 | 86.9 |
| Q3 | 16.6 | 16.6 | 16.8 | 16.6 | 70.9 | 81.1 |
| Q4 | 22.6 | 24.6 | 22.4 | 23.6 | 69.6 | 78.5 |
| Q5 | 41.4 | 42.7 | 37.2 | 42.0 | 63.1 | 79.6 |

- ▶ Model captures well that bottom 40% has almost no wealth but significant consumption share
- ▶ But **overstates consumption shares and rates of the rich.**
- ▶ Rudimentary life cycle is crucial for level of consumption rates and their decline with wealth.

Dynamics of a , y , c/y During Recession (2006-2010) across Wealth Quintiles: Data v/s Model

| a Q. | $\Delta a(\%)$ | | $\Delta y(\%)$ | | $\Delta c/y(pp)$ | |
|------|----------------|-------|----------------|-------|------------------|-------|
| | Data | Model | Data | Model | Data | Model |
| Q1 | NA | 24 | 7.4 | 4.9 | -4.4 | -0.4 |
| Q2 | 4 | 15 | 5.2 | 0.3 | -2.1 | 0.8 |
| Q3 | 6 | 8 | 2.1 | -2.4 | -0.7 | 2.2 |
| Q4 | 2 | 4 | 1.7 | -4.0 | -2.1 | 3.2 |
| Q5 | -5 | -1 | -1.1 | -6.4 | -1.6 | 4.6 |

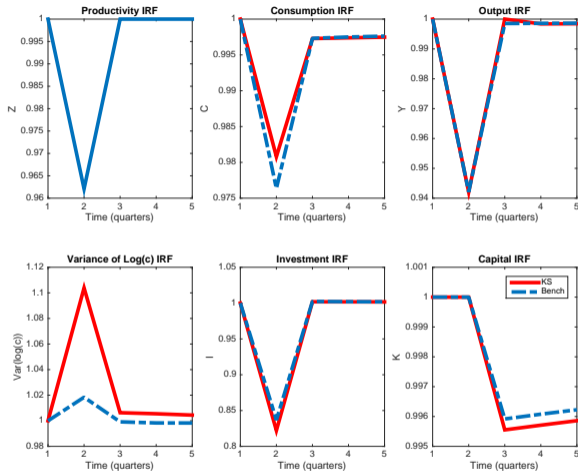
- ▷ Model's issues:
 - ▷ Model captures well that wealth-poor cut consumption rates the most.
 - ▷ Too much y fall for rich (too much mean reversion).
 - ▷ Too small decline in a at the top of wealth distribution in model (no price movements).
- ▷ Now: use the model to understand how wealth inequality matters for C , I , Y dynamics.

Inequality and the Aggregate Dynamics of a Severe Crisis

In order to understand how wealth inequality matters for C , I , Y dynamics, we compare:

- ▷ **KS economy**, with low wealth inequality (behaves \approx as RA economy)
- ▷ The calibrated **heterogenous β** (baseline) economy
- ▷ Note: calibration insures both economies have same average K/Y ratio.
- ▷ Focus on household heterogeneity and consumption dynamics in recessions shared with Guerrieri & Lorenzoni (2017), Berger & Vavra (2014), Glover, Heathcote, Krueger & Rios-Rull (2014), Heathcote & Perri (2018)

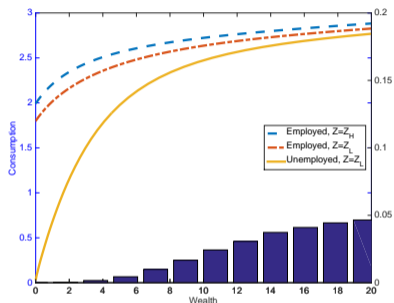
IRF, 2 Economies: One Period Recession



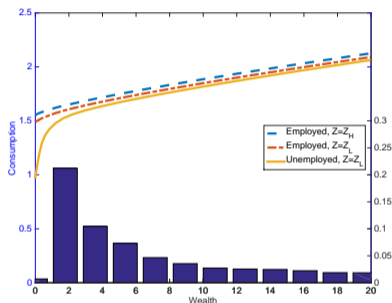
- ▷ Consumption drop: **KS -1.9%** vs **Baseline -2.4%**
- ▷ **More wealth inequality** -> to $\approx 26\%$ bigger consumption drop. **WHY?**

Consumption Functions & Wealth Distribution

KS



Het β



- ▷ **KS**: more concave consumption function (because of $\rho = 0.01$), but little mass close to $a \approx 0$
- ▷ **Benchmark** puts significant mass where consumption falls the most in recessions
- ▷ Note: households with $a \approx 0$ do not all act as hand-to-mouth (HtM) consumers. Those without job losses cut c more than y .
- ▷ Alternatives for generating high MPC households: **Wealthy HtM** [Kaplan & Violante 2014], **Durables** [Berger & Vavra 2015]

Net Worth Distributions and Consumption Decline: Different Versions of the Model

| % Share: | Models* | | | | | KS+Top 1% |
|-------------|---------|--------------|-------|------------------|-------|-----------|
| | KS | $+\sigma(y)$ | +Ret. | $+\sigma(\beta)$ | +UI | |
| Q1 | 6.9 | 0.7 | 0.7 | 0.7 | 0.3 | 5.0 |
| Q2 | 11.7 | 2.2 | 2.4 | 2.0 | 1.2 | 8.6 |
| Q3 | 16.0 | 6.1 | 6.7 | 5.3 | 4.7 | 11.9 |
| Q4 | 22.3 | 17.8 | 19.0 | 15.9 | 16.0 | 16.5 |
| Q5 | 43.0 | 73.3 | 71.1 | 76.1 | 77.8 | 57.9 |
| 90 – 95 | 10.5 | 17.5 | 17.1 | 17.5 | 17.9 | 7.4 |
| 95 – 99 | 11.8 | 23.7 | 22.6 | 25.4 | 26.0 | 8.8 |
| T1% | 5.0 | 11.2 | 10.7 | 13.9 | 14.2 | 30.4 |
| Wealth Gini | 0.350 | 0.699 | 0.703 | 0.745 | 0.767 | 0.525 |
| ΔC | -1.9% | -2.5% | -2.6% | -2.9% | -2.4% | -2.0% |

The Impact of Social Insurance Policies

- ▶ How does presence of **unemployment insurance (UI)** affect the response of **macro economy to aggregate shock**?
- ▶ **Two effects:**
 - ▶ UI moderates individual consumption decline for given wealth
 - ▶ UI changes precautionary savings incentives and thus modifies the wealth distribution
- ▶ **Two experiments:**
 - ▶ (I) Run $\rho = 0.5$ v/s $\rho = 0.1$ in benchmark economy. Both effects present.
 - ▶ (II) Hit both $\rho = 0.5$ v/s $\rho = 0.1$ economies with recession, starting with *same* wealth distribution. Isolates the first effect.

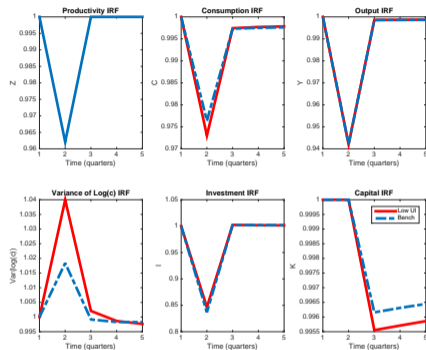
The Impact of Social Insurance Policies

- ▶ How does presence of **unemployment insurance (UI)** affect the response of **macro economy to aggregate shock**?
- ▶ **Two effects:**
 - ▶ UI moderates individual consumption decline for given wealth
 - ▶ UI changes precautionary savings incentives and thus modifies the wealth distribution
- ▶ **Two experiments:**
 - ▶ (I) Run $\rho = 0.5$ v/s $\rho = 0.1$ in benchmark economy. Both effects present.
 - ▶ (II) Hit both $\rho = 0.5$ v/s $\rho = 0.1$ economies with recession, starting with *same* wealth distribution. Isolates the first effect.
- ▶ Analysis complements **literature on impact of social insurance/tax policy on aggregate consumption dynamics in heterogeneous household models** [Heathcote 2005, Krusell & Smith 2006, McKay & Reis 2014, Kaplan & Violante 2014, Carroll, Slacalek & Tokuoka 2014, Jappelli & Pistaferri 2014, Brinca, Holter, Krusell & Malafry 2015]

The Impact of Social Insurance Policies

- ▶ How does presence of **unemployment insurance (UI)** affect the response of **macro economy to aggregate shock**?
- ▶ **Two effects:**
 - ▶ UI moderates individual consumption decline for given wealth
 - ▶ UI changes precautionary savings incentives and thus modifies the wealth distribution
- ▶ **Two experiments:**
 - ▶ (I) Run $\rho = 0.5$ v/s $\rho = 0.1$ in benchmark economy. Both effects present.
 - ▶ (II) Hit both $\rho = 0.5$ v/s $\rho = 0.1$ economies with recession, starting with *same* wealth distribution. Isolates the first effect.
- ▶ Next step would be **optimal social insurance policy analyses** in quantitative incomplete markets models [e.g. Domeij & Heathcote 2005, Conesa, Kitao & Krueger 2009, Peterman 2013, Storesletten Heathcote & Violante 2014, Karababounis 2015, Bakis, Kaymak & Poschke 2015, Krueger & Ludwig 2015, Mitman & Rabinovich 2015]

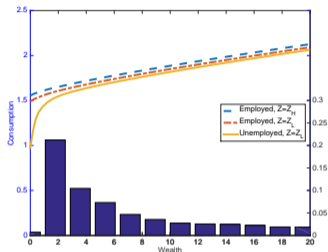
Experiment I: One Time Shock, two Levels of UI



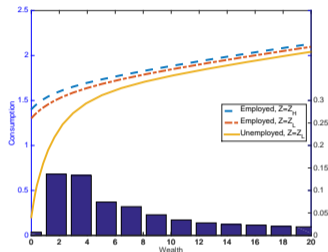
- ▷ Consumption drop: **Low UI -2.9%** vs **Baseline -2.4%**.
- ▷ Difference moderated by adjustment of wealth distribution.

Consumption Functions & Wealth Distribution

High UI

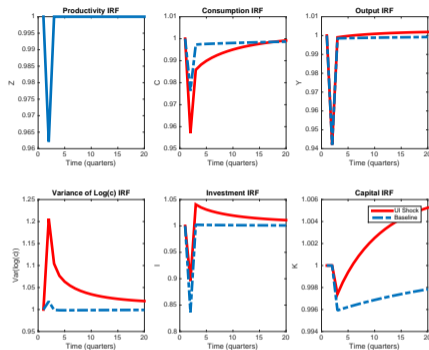


Low UI



- ▷ Benchmark: 25% with close to zero NW, compared to 15% with low UI
- ▷ Impact of UI on aggregate consumption response is muted because low UI shifts wealth distribution to right.
- ▷ How important is this effect? Suppose wealth distribution would NOT respond: **Consumption disaster!**

IRF, Fixed Distribution: One Time Shock



- ▷ Consumption drop: **Low UI -4.4%** vs **Baseline -2.4%**.
- ▷ Note: consumption would drop almost as much as output! But faster recovery.

Inequality and Aggregate Economic Activity

- ▷ So far, output Y was predetermined in the short-run
 - ▷ Z^* and N fluctuating exogenously.
 - ▷ K predetermined in short run

$$Y = Z^* K^\alpha N^{1-\alpha}$$

- ▷ Focus was on consumption C . Now: model supply and demand-side determinants of Y :
 - ▷ The supply side: Endogenizing labor supply N [not today, see also Chang & Kim 2007, Lorenzoni & Guerrieri 2017]
 - ▷ The demand side: Consumption Externality $Z^* = ZC^\omega$. Reduction in C feeds back into TFP
- ▷ Key question again: how does wealth distribution affect output dynamics now that Y is meaningfully endogenous.

A Model with an Aggregate Consumption Externality

- ▷ Now $Z^* = ZC^\omega$ with $\omega > 0$.
- ▷ Reduced form version of **real aggregate demand externalities** [e.g. Bai, Rios-Rull & Storesletten 2012, Huo & Rios-Rull 2013, Kaplan & Menzio 2014]
- ▷ Alternatively, could have introduced **nominal rigidities** making output partially demand determined [HANK Litterature]
- ▷ "Demand management" may be called for even in absence of household heterogeneity
- ▷ Social insurance policies (such as **UI**) may be desirable from **individual insurance** and **aggregate** point of view

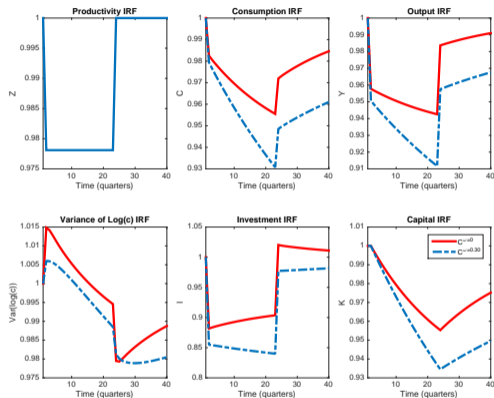
Thought Experiments

- ▶ Re-calibrate Z, ω to match output volatility
- ▶ Simulate Great Recession with externality turned on, off. *Question I*: How much amplification?
- ▶ Repeat low-UI thought experiment in $\omega > 0$ economy. *Question II*: How important is aggregate demand stabilization through UI?
- ▶ Measure welfare losses of falling into a great recession and losing job. *Question III*: How do losses depend on household characteristics, ω , UI?

Thought Experiments: Executive Summary of Answers

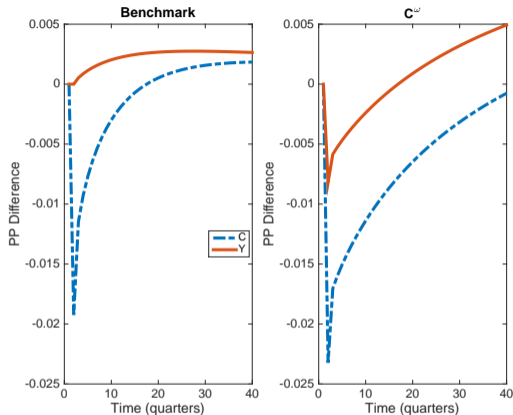
- ▶ Simulate Great Recession with externality turned on, off.
 - ▶ *Question I:* How much amplification?
 - ▶ *Answer:* Recession 2-3 pp deeper. Gap increasing over time
- ▶ Repeat low-UI thought experiment in $\omega > 0$ economy.
 - ▶ *Question II:* How important is aggregate demand stabilization through UI?
 - ▶ *Answer:* Avoids additional output recession of 1%
- ▶ Measure welfare losses of falling into a great recession and losing job.
 - ▶ *Question III:* How do losses depend on household characteristics, ω , UI?
 - ▶ *Answer:* Welfare losses very heterogeneous and large (1.5% to 11%). Have significant aggregate component. Much larger for wealth-poor if UI is small. Amplified by $\omega > 0$.

Question I: How much Amplification from $\omega > 0$?



Recession 2 – 3 pp deeper with $\omega > 0$. Gap increasing over time.

Question II: Difference in C , Y IRF with High, Low UI ($\omega = 0, \omega > 0$), Fixed Wealth Dis

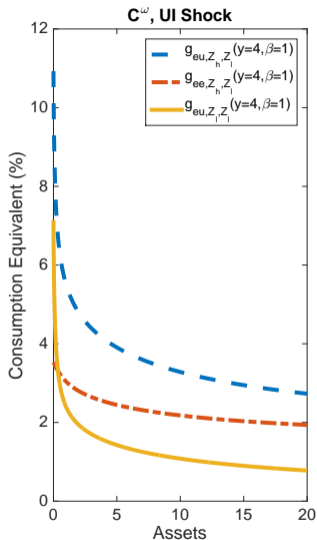
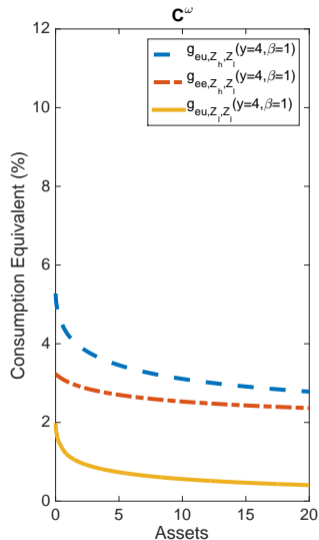


- ▷ Baseline (left panel): **Low UI** makes **consumption recession** much more severe, but no impact on **output dynamics**.
- ▷ Demand externality economy (right panel): Now **low UI** also has persistent negative effect on **output**.

Question III: What is the Size, Source of Welfare Losses from Great Recessions

- ▶ Welfare losses (% of lifetime consumption) from a great recession ($Z_h \Rightarrow Z_l$) with job loss ($e \Rightarrow u$)
 - ▶ Are large (1.5%-6%)
 - ▶ Are strongly decreasing in wealth, especially with low UI
 - ▶ Have significant aggregate component (captures aggregate wage losses and increased future unemployment risk)
 - ▶ Get larger with consumption externality and low UI (up to 11% for households with $a \approx 0$).
- ▶ Approach of calculating welfare losses of recession follows Glover, Heathcote, Krueger & Rios-Rull 2014, Hur 2014.
- ▶ Different question than welfare cost of business cycles [Lucas 1987, Krebs 2003, Krusell, Mukoyama, Sahin & Smith 2009]

Welf. Loss from Recession and Job Loss: $\omega > 0$ with High % Low UI



$$g_{eu,Z_h,Z_l}(y, a, \beta) \approx g_{ee,Z_h,Z_l}(y, a, \beta) + g_{eu,Z_l,Z_l}(y, a, \beta)$$

Conclusions: where do we stand?

- ▶ A standard Krusell-Smith model augmented by permanent preference heterogeneity does good job in matching cross-sectional **wealth distribution** (at bottom and at top).
- ▶ That model with **realistic wealth inequality** has significantly stronger **aggregate consumption** recession than low wealth inequality (or RA) economy.
- ▶ Size of **social insurance policies** can have big impact on **aggregate consumption dynamics...**
- ▶ ...and on **aggregate output** if it partially demand determined.
- ▶ although still neoclassical, model can be viewed as foundation for the HANK literature